

EENG382 HW10 – AUTHOR'S SOLUTIONS

NOTE: I have not yet verified that the author's solutions are, in fact, correct.

**Prob 17.23**

P 17.23 [a] From the solution to Problem 17.22

$$H(\omega) = \frac{2}{j\omega + 2}$$

Now,

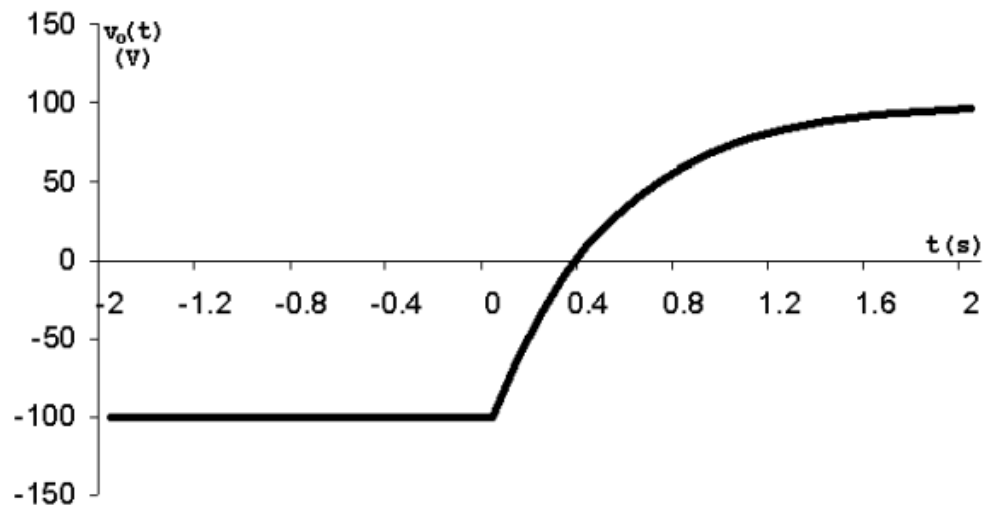
$$V_g(\omega) = \frac{200}{j\omega}$$

Then,

$$V_o(\omega) = H(\omega)V_g(\omega) = \frac{400}{j\omega(j\omega + 2)} = \frac{K_1}{j\omega} + \frac{K_2}{j\omega + 2} = \frac{200}{j\omega} - \frac{200}{j\omega + 2}$$

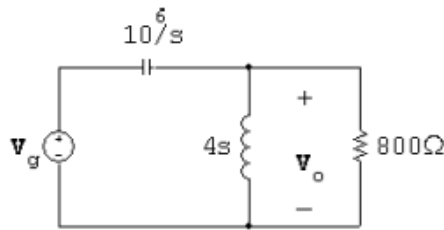
$$\therefore v_o(t) = 100\text{sgn}(t) - 200e^{-2t}u(t) \text{ V}$$

[b]



**Prob 17.32**

P 17.32 [a]



$$\frac{(V_o - V_g)s}{10^6} + \frac{V_o}{4s} + \frac{V_o}{800} = 0$$

$$\therefore V_o = \frac{s^2 V_g}{s^2 + 1250s + 25 \times 10^4}$$

$$\frac{V_o}{V_g} = H(s) = \frac{s^2}{(s + 250)(s + 1000)}$$

$$H(j\omega) = \frac{(j\omega)^2}{(j\omega + 250)(j\omega + 1000)}$$

$$v_g = 45e^{-500|t|}; \quad V_g(\omega) = \frac{45,000}{(j\omega + 500)(-j\omega + 500)}$$

$$\begin{aligned} \therefore V_o(\omega) &= H(j\omega)V_g(\omega) = \frac{45,000(j\omega)^2}{(j\omega + 250)(j\omega + 500)(j\omega + 1000)(-j\omega + 500)} \\ &= \frac{K_1}{j\omega + 250} + \frac{K_2}{j\omega + 500} + \frac{K_3}{j\omega + 1000} + \frac{K_4}{-j\omega + 500} \end{aligned}$$

$$K_1 = \frac{45,000(-250)^2}{(250)(750)(750)} = 20$$

$$K_2 = \frac{45,000(-500)^2}{(-250)(500)(1000)} = -90$$

$$K_3 = \frac{45,000(-1000)^2}{(-750)(-500)(1500)} = 80$$

$$K_4 = \frac{45,000(500)^2}{(750)(1000)(1500)} = 10$$

$$\therefore v_o(t) = [20e^{-250t} - 90e^{-500t} + 80e^{-1000t}]u(t) + 10e^{500t}u(-t) \text{ V}$$

**Prob 17.32 (Cont'd)**

$$[\mathbf{b}] \quad v_o(0^-) = 10 \text{ V}; \quad V_o(0^+) = 20 - 90 + 80 = 10 \text{ V}$$

$$v_o(\infty) = 0 \text{ V}$$

$$[\mathbf{c}] \quad I_L = \frac{V_o}{4s} = \frac{0.25sV_g}{(s+250)(s+1000)}$$

$$H(s) = \frac{I_L}{V_o} = \frac{0.25s}{(s+250)(s+1000)}$$

$$H(j\omega) = \frac{0.25(j\omega)}{(j\omega+250)(j\omega+1000)}$$

$$\begin{aligned} I_L(\omega) &= \frac{0.25(j\omega)(45,000)}{(j\omega+250)(j\omega+500)(j\omega+1000)(-j\omega+500)} \\ &= \frac{K_1}{j\omega+250} + \frac{K_2}{j\omega+500} + \frac{K_3}{j\omega+1000} + \frac{K_4}{-j\omega+500} \end{aligned}$$

$$K_4 = \frac{(0.25)(500)(45,000)}{(750)(1000)(1500)} = 5 \text{ mA}$$

$$i_L(t) = 5e^{500t}u(-t); \quad \therefore i_L(0^-) = 5 \text{ mA}$$

$$K_1 = \frac{(0.25)(-250)(45,000)}{(250)(750)(750)} = -20 \text{ mA}$$

$$K_2 = \frac{(0.25)(-500)(45,000)}{(-250)(500)(1000)} = 45 \text{ mA}$$

$$K_3 = \frac{(0.25)(-1000)(45,000)}{(-750)(-500)(1500)} = -20 \text{ mA}$$

$$\therefore i_L(0^+) = K_1 + K_2 + K_3 = -20 + 45 - 20 = 5 \text{ mA}$$

Checks, i.e.,  $i_L(0^+) = i_L(0^-) = 5 \text{ mA}$

At  $t = 0^-$ :

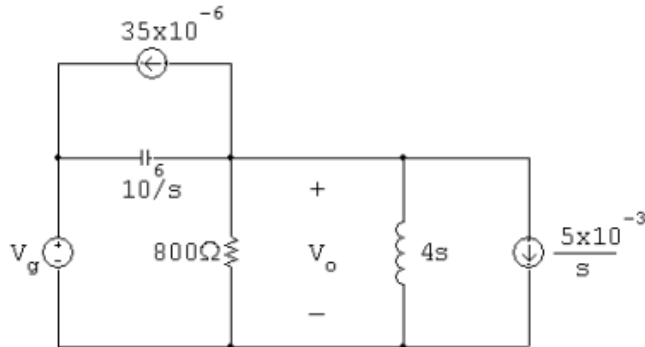
$$v_C(0^-) = 45 - 10 = 35 \text{ V}$$

At  $t = 0^+$ :

$$v_C(0^+) = 45 - 10 = 35 \text{ V}$$

**Prob 17.32 (Cont'd)**

[d] We can check the correctness of our solution for  $t \geq 0^+$  by using the Laplace transform. Our circuit becomes



$$\frac{V_o}{800} + \frac{V_o}{4s} + \frac{(V_o - V_g)s}{10^6} + 35 \times 10^{-6} + \frac{5 \times 10^{-3}}{s} = 0$$

$$\therefore (s^2 + 1250s + 24 \times 10^4)V_o = s^2V_g - (35s + 5000)$$

$$v_g(t) = 45e^{-500t}u(t) \text{ V}; \quad V_g = \frac{45}{s + 500}$$

$$\therefore (s + 250)(s + 1000)V_o = \frac{45s^2 - (35s + 5000)(s + 500)}{(s + 500)}$$

$$\begin{aligned} \therefore V_o &= \frac{10s^2 - 22,500s - 250 \times 10^4}{(s + 250)(s + 500)(s + 1000)} \\ &= \frac{20}{s + 250} - \frac{90}{s + 500} + \frac{80}{s + 1000} \end{aligned}$$

$$\therefore v_o(t) = [20e^{-250t} - 90e^{-500t} + 80e^{-1000t}]u(t) \text{ V}$$

This agrees with our solution for  $v_o(t)$  for  $t \geq 0^+$ .

**Prob 17.36**

$$\text{P 17.36 } V_o(s) = \frac{10}{s} + \frac{30}{s+20} - \frac{40}{s+30} = \frac{600(s+10)}{s(s+20)(s+30)}$$

$$V_o(s) = H(s) \cdot \frac{15}{s}$$

$$\therefore H(s) = \frac{40(s+10)}{(s+20)(s+30)}$$

$$\therefore H(j\omega) = \frac{40(j\omega+10)}{(j\omega+20)(j\omega+30)}$$

$$\therefore V_o(j\omega) = \frac{30}{j\omega} \cdot \frac{40(j\omega+10)}{(j\omega+20)(j\omega+30)} = \frac{1200(j\omega+10)}{j\omega(j\omega+20)(j\omega+30)}$$

$$v_o(j\omega) = \frac{20}{j\omega} + \frac{60}{j\omega+20} - \frac{80}{j\omega+30}$$

$$v_o(t) = 10\text{sgn}(t) + [60e^{-20t} - 80e^{-30t}]u(t) \text{ V}$$