

EENG 281 Homework #11 Solutions
Fall 2013

P 9.11 [a] $\mathbf{Y} = 50/\underline{60^\circ} + 100/\underline{-30^\circ} = 111.8/\underline{-3.43^\circ}$

$$y = 111.8 \cos(500t - 3.43^\circ)$$

[b] $\mathbf{Y} = 200/\underline{50^\circ} - 100/\underline{60^\circ} = 102.99/\underline{40.29^\circ}$

$$y = 102.99 \cos(377t + 40.29^\circ)$$

[c] $\mathbf{Y} = 80/\underline{30^\circ} - 100/\underline{-225^\circ} + 50/\underline{-90^\circ} = 161.59/\underline{-29.96^\circ}$

$$y = 161.59 \cos(100t - 29.96^\circ)$$

[d] $\mathbf{Y} = 250/\underline{0^\circ} + 250/\underline{120^\circ} + 250/\underline{-120^\circ} = 0$

$$y = 0$$

P 9.12 [a] $\mathbf{V}_g = 300/\underline{78^\circ}$; $\mathbf{I}_g = 6/\underline{33^\circ}$

$$\therefore Z = \frac{\mathbf{V}_g}{\mathbf{I}_g} = \frac{300/\underline{78^\circ}}{6/\underline{33^\circ}} = 50/\underline{45^\circ} \Omega$$

[b] i_g lags v_g by 45° :

$$2\pi f = 5000\pi; \quad f = 2500 \text{ Hz}; \quad T = 1/f = 400 \mu\text{s}$$

$$\therefore i_g \text{ lags } v_g \text{ by } \frac{45^\circ}{360^\circ}(400 \mu\text{s}) = 50 \mu\text{s}$$

P 9.27 $Z_{ab} = 1 - j8 + (2 + j4) \parallel (10 - j20) + (40 \parallel j20)$

$$= 1 - j8 + 3 + j4 + 8 + j16 = 12 + j12 \Omega = 16.97/\underline{45^\circ} \Omega$$

$$\text{P 9.28 } \mathbf{V}_g = 40/\underline{-15^\circ} \text{ V}; \quad \mathbf{I}_g = 40/\underline{-68.13^\circ} \text{ mA}$$

$$Z = \frac{\mathbf{V}_g}{\mathbf{I}_g} = 1000/\underline{53.13^\circ} \Omega = 600 + j800 \Omega$$

$$Z = 600 + j \left(3.2\omega - \frac{0.4 \times 10^6}{\omega} \right)$$

$$\therefore 3.2\omega - \frac{0.4 \times 10^6}{\omega} = 800$$

$$\therefore \omega^2 - 250\omega - 125,000 = 0$$

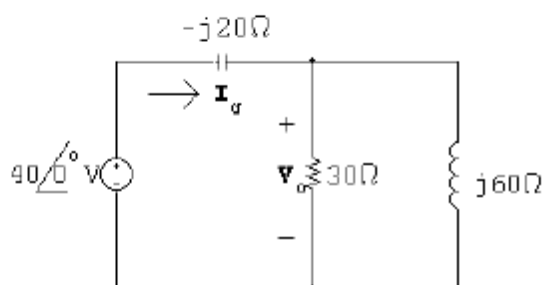
Solving,

$$\omega = 500 \text{ rad/s}$$

$$\text{P 9.29} \quad \frac{1}{j\omega C} = \frac{1}{(1 \times 10^{-6})(50 \times 10^3)} = -j20 \Omega$$

$$j\omega L = j50 \times 10^3(1.2 \times 10^{-3}) = j60 \Omega$$

$$\mathbf{V}_g = 40\angle 0^\circ \text{ V}$$



$$Z_e = -j20 + 30\|j60 = 24 - j8 \Omega$$

$$\mathbf{I}_g = \frac{40\angle 0^\circ}{24 - j8} = 1.5 + j0.5 \text{ mA}$$

$$\mathbf{V}_o = (30\|j60)\mathbf{I}_g = \frac{30(j60)}{30 + j60}(1.5 + j0.5) = 30 + j30 = 42.43\angle 45^\circ \text{ V}$$

$$v_o = 42.43 \cos(50,000t + 45^\circ) \text{ V}$$